

## Central Contribution

We present a theory of phonology based on the computational properties of input-output mappings. These properties define restrictive classes of mappings which are learnable by a provably correct, efficient algorithm. The algorithm learns both the active surface constraints and the repairs, including opaque mappings.

## Introduction

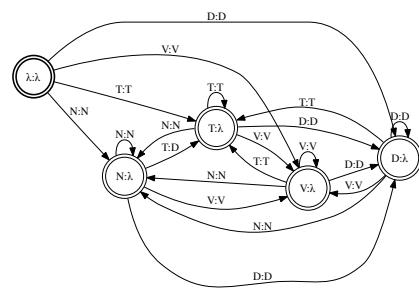
- Output-oriented theories of phonological grammars are in part motivated by ‘conspiracies’ in which the same marked structure is targeted by a range of different processes.

- (1) Fusion (Indonesian)  
/məN+pilih/ → [məmilih], ‘to choose’
- (2) Voicing (Quechua)  
/kam+pa/ → [kamba], ‘yours’
- (3) Denasalization (Toba Batak) (Hayes, 1986)  
/maʒinim tuak/ → [maʒinup tuak], ‘drink palm wine’

- In OT a single markedness constraint (\*NC) ranked with respect to a set of faithfulness constraints accounts for this variation (Pater, 2004).
- We likewise propose a learner that separates the marked structure and the repair and can furthermore learn opaque input-output mappings.

## Computational Approach

- Both rule- and constraint-based theories of generative phonology concur on the existence of a mapping from input (underlying) to output (surface) forms.
- We model these mappings with *functions* with the goal of identifying computational properties that are independent of these grammatical formalisms (i.e., rules and constraints).
- (4)  $f(\text{kam+pa}) = [\text{kamba}]$
- In particular, identifying the most *restrictive* computational properties leads us to a better characterization of the components of phonological grammars (Johnson, 1972; Kaplan and Kay, 1994; Mohri, 1997).
- FSTs are a finite means of representing an infinite function like (4).



	k	a	m	p	a	#
λ	⇒ T	⇒ V	⇒ N	⇒ T	⇒ V	⇒ λ
	k	a	m	b	a	λ

Figure 1: Quechua obstruent voicing

- This FST belongs to a restricted class called *Input Strictly Local* (ISL ⊂ Subsequential ⊂ Regular) (Mohri, 1997; Chandlee, 2014; Chandlee et al., 2014).

## The Algorithm

- **Structured Onward Subsequential Function Inference Algorithm (SOSFIA)** (Jardine et al., 2014)
- Input: set of input/output pairs (data) and an **output-empty subsequent FST (eFST)** (structure)

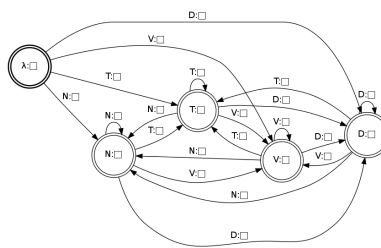
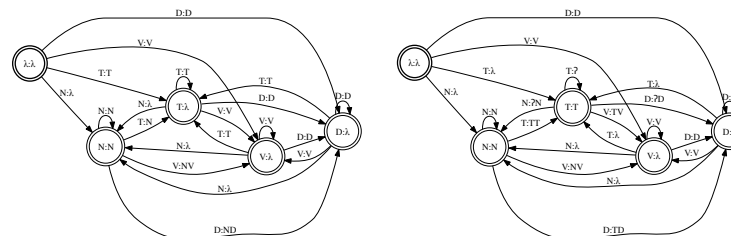


Figure 2: An output-empty FST for learning repairs with T, D, V, and N

- SOSFIA uses data input/output pairs to fill in the *blank outputs* of the eFST.
- The eFST defines the *class of functions* in the range of the learner.



Indonesian fusion

Toba Batak denasalization

Figure 3: Two FSTs in range of SOSFIA, given Figure 2

- In a phonological context, this determines the *range of constraints* for which it is possible to learn repairs—with Figure 2, SOSFIA only learns *local* constraints concerning the natural classes of vowels, nasals, and voiced and voiceless obstruents.

## Advantages

- Provably learns any transduction in the class defined by eFST from positive data.
- Like ISLFLA of Chandlee (2014); Chandlee et al. (2014), but uses knowledge of structure to be very efficient: the learner is fast (linear in size of input) and requires a small amount of data (linear in size of eFST).
- Consistent with research showing phonological processes to be subsequential (Chandlee and Heinz, 2012; Heinz and Lai, 2013; Payne, 2014), with the majority in the more restrictive ISL class (Chandlee, 2014).
- Learns opaque processes without recourse to intermediate representations (see Figure 3).
- Can learn long-distance phenomena if supplied the correct eFST

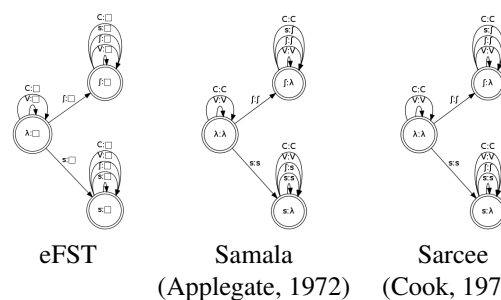


Figure 4: FSTs for long-distance sibilant harmony typology

## Discussion

- The eFST represents the learner’s *a priori* knowledge about the target mapping it is trying to learn.
- When the target is part of a highly-structured class of mappings (such as the ISL ones), this *a priori* knowledge greatly facilitates learning.
- In the case of phonology, a process is ISL provided it can be described with a rule that applies simultaneously in which the target and triggering context are a contiguous substring of bounded length (Chandlee, 2014; Chandlee and Heinz, 2014).
- Like classical OT,
  - 1) there are no intermediate representations,
  - 2) the constraints are given *a priori* (here in the structure of the class), and
  - 3) we can provide strong learnability results.
- Unlike classical OT,
  - 1) opaque mappings are representable and learnable,
  - 2) non-regular mappings cannot be generated (cf. Riggle, 2004; Gerdemann and Hulden, 2012).

## Future and Ongoing Work

- One of these classes, the ISL class, is well defined (Chandlee, 2014; Chandlee et al., 2014). Non-local classes (such as in Figure 4) are not well understood. What non-local class(es) is (are) there? How do they relate to the ISL class?
- Given that there are multiple classes towards which human learners are biased, they learn different kinds of mappings. How are these mappings composed into a single, unified phonology? This is a different question than the ‘rule-ordering’ composition of, ex., Kaplan and Kay (1994).
- Given that optimization of simple constraints under particular rankings can result in complex mappings (Riggle, 2004; Gerdemann and Hulden, 2012), it appears unlikely that OT can account for the computational properties of phonological mappings mentioned here, but this certainly deserves further investigation.

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